

RC-Run.mw

```

> read `/home/ph/maple/RC.txt`:read "/home/ph/maple/cartan.txt";unprotect(gamma);

> with(PolynomialTools):

> read `/home/ph/maple/Solv.txt`;

      "UT(R,B) will simultaneously upper-triangularize two Matrices R and B"

> unassign('x');

> R:=transmat([12,12,10,10,3,8,6,6,4,4,2,1,12,15,14]):B:=transmat([11,11,5,9,9,7,5,2,7,1,8,3]): #***** 15 *****

> R:=transmat([12,12,10,10,3,8,6,6,4,4,2,1]):B:=transmat([11,11,5,9,9,7,5,2,7,1,8,3]): #***** 16 *****

> R:=transmat([12,12,12,10,10,10,6,5,7,5,6,2]):B:=transmat([10,11,9,9,8,8,5,3,4,1,5,3]): #***** 12 *****RG
=====2S dbly stoch=====SW sandwich=====
> R:=transmat([2,4,4,6,6,2]):B:=transmat([3,1,5,3,1,5]): #rank 6; 32-41-45-63-61-25 RG CC SW

> R:=transmat([3,3,5,5,1,1]):B:=transmat([2,4,6,6,4,2]): #rank 6;-- gamma 331/2048 RG CC SW

> unassign('a','b','c'): R:=transmat([c,c,a,a,3,8,6,6,4,4,8,a]):B:=transmat([b,b,5,9,9,7,5,2,7,1,2,1]): #***** 12
*****RG CC sync

> R:=transmat([12,12,10,10,3,8,6,6,4,4,8,3]):B:=transmat([11,11,5,9,9,7,5,2,7,1,2,1]): #***** 12 *****RG

> R:=transmat([8,8,b,7,7,5,5,4,4,3,1,2]):B:=transmat([c,b,a,9,8,7,6,5,3,4,2,1]): #***** 12 *****
RG-CHECKED

> unassign('a','b','c'): R:=transmat([c,c,1,2,4,1,5,5,1,2,1,1]):B:=transmat([7,b,8,3,9,a,6,6,a,9,9,a]): #rank 9; CHECKED ***
BIG 12 ** CC sync

> R:=transmat([4,4,4,7,7,7,1,1,1]):B:=transmat([2,9,5,8,3,8,5,6,2]): #rank 9; 42-49-45-78-73-78-15-16-12 *** NINER *** Big
NCC SW

> R:=transmat([2,7,8,2,4,8,6,6]):B:=transmat([3,1,1,3,3,1,5,5]): #rank 5; 23-71-81-23-43-81-65-65 RG

> R:=transmat([2,1,1,2,4,1,5,5]):B:=transmat([3,7,8,3,3,8,6,6]): #rank 5; 23-17-18-23-43-18-56-56 *****8***** RG CC
ONLY RIGHT GROUPS***

> R:=transmat([2,3,2,2,1,3]):B:=transmat([5,4,6,5,4,5]): #rank 5 25-34-26-52-41-53 RG CC

> R:=transmat([2,3,1,1,2,4]):B:=transmat([3,1,4,5,6,3]): #rank 5; 23-31-14-51-62-43 RG checked INVERTIBLE WITH A
RIGHT GROUP***** NOT CC

> R:=transmat([3,5,5,1,7,8,8,7]):B:=transmat([4,6,2,5,6,1,5,6]): #rank 6; ## CHECKED RG-CHECKED NOT CC

> R:=transmat([2,1,1,2,3,1,5,5]):B:=transmat([6,7,8,6,4,8,4,7]): #rank 6; 26-17-18-62-43-81-54-57 RG-CHECKED CC

> R:=transmat([2,1,1,2,4,1,5,5]):B:=transmat([3,7,8,3,3,8,6,6]): #rank 5;RG-CHECKED

> R:=transmat([3,3,5,6,7,7,1,2]):B:=transmat([2,4,4,5,6,8,8,1]): # 32-34-54-56-76-78-18-12 CHECKED RG

> R:=transmat([2,4,4,2,1,4]):B:=transmat([3,6,5,3,6,5]):#rank 4 / CC 23-46-45-23-61-54 ***** recolored
244265-365314 ***** RG

> R:=transmat([6,1,5,6,1,5]):B:=transmat([2,5,1,2,3,4]): #rank 5 / CC 62-15-51-62-13-54 --- RG-CHECKED

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> R:=transmat([2,3,1,3]):B:=transmat([4,4,2,2]): #rank 3, A invertible 24-34-12-32 --- RG-CHECKED ***** 2313-4422
*****

> R:=transmat([2,3,2,3]):B:=transmat([4,4,1,1]):#rank 3 &CC --- same as 3311-2442 Mini-SW

> R:=transmat([4,4,4,2]):B:=transmat([3,3,1,3]):#rank 3 / CC 43-34-14-23 --- checked for Delta
*****4*****CC*

> R:=transmat([2,6,4,2,6,4]):B:=transmat([5,5,1,1,3,3]): # 25-65-41-21-63-43 --- RG-CHECKED

> R:=transmat([4,4,1,1,7,7,3,4]):B:=transmat([5,6,2,2,8,8,2,6]): #rank 5 & CC CHECKED

> R:=transmat([5,4,2,2,3]):B:=transmat([3,3,1,5,4]): #rank 4 / RG-CHECKED

> R:=transmat([5,3,1,5,3,1]):B:=transmat([6,4,2,6,4,2]): #rank 3 / CC 56-34-12-56-34-12 RG-CHECKED 2S

> R:=transmat([5,4,4,2,6,5]):B:=transmat([3,6,5,3,1,4]): RG-CHECKED

> R:=transmat([5,5,1,6,3,3]):B:=transmat([4,4,6,1,2,2]):# rank 3 54-54-16-61-32-32 2S

> R:=transmat([2,3,2,2,3]):B:=transmat([1,4,1,5,4]): # RG-CHECKED

> R:=transmat([4,5,1,6,3,2]):B:=transmat([5,4,6,1,2,3]):# rank 3 RG-CHECKED

> R:=transmat([3,3,5,5,1,2]):B:=transmat([4,4,6,6,2,3]):# rank 3 RG-CHECKED

> R:=transmat([3,3,5,5,1,1]):B:=transmat([2,4,4,6,6,2]):# 32-34-54-56-16-12 RG-CHECKED 2S

> R:=transmat([3,4,6,5,1,2]):B:=transmat([4,3,5,6,2,3]):# 34-43-65-56-12-23 RG-CHECKED

> R:=transmat([4,6,6,3,3,1,2]):B:=transmat([5,7,7,5,4,2,1]): # a SEVEN NO RG's other than groups RG-CHECKED

> R:=transmat([3,4,5,5,1]):B:=transmat([2,3,1,1,4]): #rank 4 / CC 32-43-51-51-14 RG-CHECKED

> R:=transmat([3,4,1,5,4]):B:=transmat([2,3,5,1,1]): #rank 4 / CC RG-CHECKED

> R:=transmat([6,1,1,6,1,4]):B:=transmat([2,5,5,2,3,5]):# RG-CHECKED

> R:=transmat([2,1,5,5,1]):B:=transmat([4,3,4,3,2]):# A invertible RG-CHECKED 2S

> R:=transmat([3,3,5,5,1,1]):B:=transmat([2,4,6,6,4,2]): #rank 6; RG-CHECKED 2S

> R:=transmat([6,1,5,2,3,4]):B:=transmat([2,5,1,6,1,5]): #rank 6; RG-CHECKED

> R:=transmat([2,4,2,3]):B:=transmat([4,3,1,1]): # XXX

> R:=transmat([2,1,2,1]):B:=transmat([4,3,4,3]): # XXX

> R:=transmat([4,4,6,6,2,2]):B:=transmat([5,5,1,1,3,3]): # RG-CHECKED 17/32 not sync'd 2S

> R:=transmat([2,3,4,5,6,7,8,9,1]):B:=transmat([5,6,7,2,3,4,5,6,7]): #RG-CHECKED Recolors to rank 6 RG PERIODIC

> R:=transmat([3,3,1,1,7,7,5,5]):B:=transmat([6,8,8,6,2,4,4,2]): #BIG 8

> R:=transmat([2,3,1]):B:=transmat([3,1,2]):# RG-CHECKED

> R:=transmat([1,1,2,2,2]):B:=transmat([3,4,4,5,4]): # CC with a rank 4 RG and rank 2 RG

> R:=transmat([9,3,5,1,7,2,6,7,9]):B:=transmat([6,4,9,2,5,8,1,9,4]): #INVERTIBLE RG-CHECKED all sync

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> unassign('a','b','c'):R:=transmat([9,4,4,7,7,7,1,1,1,a]):B:=transmat([3,9,a,8,3,1,5,6,2,1]): #RG-CHECKED
> unassign('a','b','c'):R:=transmat([3,3,3,7,7,7,b,b,2,4,9]):B:=transmat([6,6,6,a,a,a,c,c,c,1,5,8]): #
> R:=transmat([6,2,5,3,3,1,7]):B:=transmat([2,4,7,5,2,5,1]): #
> R:=transmat([2,3,1,3]):B:=transmat([4,4,4,2]): # INVERTIBLE
> R:=transmat([1,4,2,2,2]):B:=transmat([2,1,4,5,3]): # INVERTIBLE with RANK 3 RG
> R:=transmat([5,7,2,2,5,3,3]):B:=transmat([7,3,4,6,2,1,5]): #
> unassign('a','b','c','d'):R:=transmat([1,1,1,1,2,2,2,2,3,3,3,3]):B:=transmat([c,b,a,6,c,7,4,5,c,8,9,7]): #TESTER
> ##### START HERE #####
> Delta:=evalm((R-B)/2):A:=evalm((R+B)/2):
  `R`=matrans(R); `B`=matrans(B);pi:=nullspace(J-transpose(A)):c:=add(pi[1][k],k=1..n):pi:=evalm(pi[1]/c);Omega:=stackma
> NN:=binomial(n,2):J2:=evalm(IdentityMatrix(NN)):uu:=vector(NN,1):unassign('t','e','x','tau'):t:=vector(n):phi:=diag(seq(t
> d:=rank(Delta):`rank of Delta`=d,`for n equals`=n;`rank of
  A`=rank(A);#NA:=NullSpace(Matrix(A)):NTA:=NullSpace(Matrix(transpose(A))):nu:=nullity(Delta):zeta:=vector(n,0):u=
  A",det(A),"nullspace",evalm(1/x[1]*linsolve(A,vector(n,0),'rr',x)),"ker DELTA",nullspace(Delta);"A",factor(det(J-lambda*
  one-half",evalm(1/x[1]*linsolve(2*A-J,vector(n,0),'rr',x)));"eigenvalue A minus
  one-half",evalm(1/x[1]*linsolve(2*A+J,vector(n,0),'rr',x)));"Delta",factor(det(J-lambda*Delta)));"eigenvalue Delta plus
  one-half",evalm(1/x[1]*linsolve(2*Delta-J,vector(n,0),'rr',x)));"eigenvalue Delta minus one-half",evalm(1/x[1]*linsolve(2*D
> print();if(rank(A)=rank(Delta)) then print("<--> CC <-->") else print("NOT CC", "RANKDIFF",rank(A)-rank(Delta))
  fi;print();NSA:=nullspace(A);"DIM NULLSPACE OF A",nops(NSA);

      R = [3, 3, 3, 7, 7, 7, B, B, B, 2, 4, 9]
      B = [6, 6, 6, A, A, A, C, C, C, 1, 5, 8]
      pi := [ 1/18, 1/18, 1/9, 1/18, 1/18, 1/9, 1/9, 1/18, 1/18, 1/9, 1/9, 1/9 ]

      rank of Delta = 6, for n equals = 12

      rank of A = 6

      "<--> CC <-->"<--> CC <-->" align="center">

NSA := {[0, 0, -1, 0, 0, 1, 0, 0, 0, 0, 0, 0], [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, -1], [0, 0, 0, 0, 0, 0, 1, 0, 0, -1, 0, 0],
  [0, 0, 0, 0, 0, 0, 0, 1, -1, 0, 0, 0], [0, 0, 0, -1, 1, 0, 0, 0, 0, 0, 0, 0], [1, -1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]}

      "DIM NULLSPACE OF A", 6

> print("PERIODICITY CHECK",nullspace(evalm(sympow(J,2)-sympow(A,2)))));

      "PERIODICITY CHECK", {}

=====

> if(rank(A)>rank(Delta)) then print("CONTINUE AT THE MAIN RUN") fi;
> unassign('a'):typ:=linsolve(A,vector(n,0),'rr',a);

      typ := [-a1, a1, -a2, -a5, a5, a2, -a4, -a3, a3, a4, a6, -a6]

> a[1]:=1:a[2]:=1:a[3]:=1:a[4]:=1:a[5]:=1:a[6]:=-1:
> for k from 0 to 6 do for i in choose(6,k) do a:=vector(6,1): if (1 in i) then next fi;for j to 6 do if(j in i) then a[j]:=-1 fi od;

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> colr:={}:g:=map(eval,typ);gmat:=diag(seq(g[k],k=1..n)):
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> Detta:=evalm(gmat&*A&*gmat):R:=evalm(A+Detta):B:=evalm(A-Detta):mr:=matrans(R):ex:={}:ey:={}:for i to n do
if(mr[i]<>MR[i]) then ex:=ex union {i} else ey:=ey union {i} fi;od;print("a",a,"g",g);print("coloring",ex,ey);if([ex,2] in
two) then print("X2") fi; if ([ey,2] in two) then print("Y2") fi;od;od;
```

```
"a", [1, 1, 1, 1, 1, 1], "g", [-1, 1, -1, -1, 1, 1, -1, -1, 1, 1, 1, -1]
```

```
"coloring", {2, 5, 6, 7, 8, 11, 12}, {1, 3, 4, 9, 10}
```

```
"X2"
```

```
"a", [1, -1, 1, 1, 1, 1], "g", [-1, 1, 1, -1, 1, -1, -1, -1, 1, 1, 1, -1]
```

```
"coloring", {1, 5, 7, 8, 11, 12}, {2, 3, 4, 6, 9, 10}
```

```
"Y2"
```

```
"a", [1, 1, -1, 1, 1, 1], "g", [-1, 1, -1, -1, 1, 1, -1, 1, -1, 1, 1, -1]
```

```
"coloring", {2, 5, 6, 7, 9, 11}, {1, 3, 4, 8, 10, 12}
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"a", [1, 1, 1, -1, 1, 1], "g", [-1, 1, -1, -1, 1, 1, 1, -1, 1, -1, 1, -1]
```

```
"coloring", {2, 4, 8, 10, 11, 12}, {1, 3, 5, 6, 7, 9}
```

```
"X2"
```

```
"a", [1, 1, 1, 1, -1, 1], "g", [-1, 1, -1, 1, -1, 1, -1, -1, 1, 1, 1, -1]
```

```
"coloring", {2, 4, 6, 7, 8, 12}, {1, 3, 5, 9, 10, 11}
```

```
"X2"
```

```
"a", [1, 1, 1, 1, 1, -1], "g", [-1, 1, -1, -1, 1, 1, -1, -1, 1, 1, -1, 1]
```

```
"coloring", {2, 5, 6, 9}, {1, 3, 4, 7, 8, 10, 11, 12}
```

```
"X2"
```

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"a", [1, -1, -1, 1, 1, 1], "g", [-1, 1, 1, -1, 1, -1, -1, 1, -1, 1, 1, -1]
```

```
"coloring", {1, 5, 7, 9, 11}, {2, 3, 4, 6, 8, 10, 12}
```

```
"Y2"
```

```
"a", [1, -1, 1, -1, 1, 1], "g", [-1, 1, 1, -1, 1, -1, 1, -1, 1, -1, 1, -1]
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"coloring", {1, 4, 6, 8, 10, 11, 12}, {2, 3, 5, 7, 9}
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"Y2"
```

```
"a", [1, -1, 1, 1, -1, 1], "g", [-1, 1, 1, 1, -1, -1, -1, -1, 1, 1, 1, -1]
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"coloring", {1, 4, 7, 8, 12}, {2, 3, 5, 6, 9, 10, 11}
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"Y2"
```

```
"a", [1, -1, 1, 1, 1, -1], "g", [-1, 1, 1, -1, 1, -1, -1, -1, 1, 1, -1, 1]
```

```
"coloring", {1, 5, 9}, {2, 3, 4, 6, 7, 8, 10, 11, 12}
```

```
"Y2"
```

```
"a", [1, 1, -1, -1, 1, 1], "g", [-1, 1, -1, -1, 1, 1, 1, 1, -1, -1, 1, -1]
```

```
"coloring", {2, 4, 9, 10, 11}, {1, 3, 5, 6, 7, 8, 12}
```

```

"X2"
"a", [1, 1, -1, 1, -1, 1], "g", [-1, 1, -1, 1, -1, 1, -1, 1, -1, 1, 1, -1]
    "coloring", {2, 4, 6, 7, 9}, {1, 3, 5, 8, 10, 11, 12}
"X2"
"a", [1, 1, -1, 1, 1, -1], "g", [-1, 1, -1, -1, 1, 1, -1, 1, -1, 1, -1, 1]
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"a", [1, 1, 1, -1, -1, 1], "g", [-1, 1, -1, 1, -1, 1, 1, -1, 1, -1, 1, -1]
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"a", [1, 1, 1, -1, 1, -1], "g", [-1, 1, -1, -1, 1, 1, 1, -1, 1, -1, -1, 1]
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"a", [1, 1, 1, 1, -1, -1], "g", [-1, 1, -1, 1, -1, 1, -1, -1, 1, 1, -1, 1]
    "coloring", {2, 4, 6, 9, 11}, {1, 3, 5, 7, 8, 10, 12}
"X2"
"a", [1, -1, -1, -1, 1, 1], "g", [-1, 1, 1, -1, 1, -1, 1, 1, -1, -1, 1, -1]
    "coloring", {1, 4, 6, 9, 10, 11}, {2, 3, 5, 7, 8, 12}
"Y2"
"a", [1, -1, -1, 1, -1, 1], "g", [-1, 1, 1, 1, -1, -1, -1, 1, -1, 1, 1, -1]
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    "coloring", {1, 4, 6, 7, 9, 10}, {2, 3, 5, 8, 11, 12}
"Y2"
"a", [1, -1, 1, 1, -1, -1], "g", [-1, 1, 1, 1, -1, -1, -1, -1, 1, 1, -1, 1]
    "coloring", {1, 4, 9, 11}, {2, 3, 5, 6, 7, 8, 10, 12}
"Y2"
"a", [1, 1, -1, -1, -1, 1], "g", [-1, 1, -1, 1, -1, 1, 1, 1, -1, -1, 1, -1]

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"coloring", {2, 5, 9, 10}, {1, 3, 4, 6, 7, 8, 11, 12}
"X2"
"a", [1, 1, -1, -1, 1, -1], "g", [-1, 1, -1, -1, 1, 1, 1, 1, -1, -1, -1, 1]
"coloring", {2, 4, 7, 8, 10, 12}, {1, 3, 5, 6, 9, 11}
"X2"
"a", [1, 1, -1, 1, -1, -1], "g", [-1, 1, -1, 1, -1, 1, -1, 1, -1, 1, -1, 1]
"coloring", {2, 4, 6, 8, 11, 12}, {1, 3, 5, 7, 9, 10}
"X2"
"a", [1, 1, 1, -1, -1, -1], "g", [-1, 1, -1, 1, -1, 1, 1, -1, 1, -1, -1, 1]
"coloring", {2, 5, 7, 9, 10, 11}, {1, 3, 4, 6, 8, 12}
"X2"
"a", [1, -1, -1, -1, -1, 1], "g", [-1, 1, 1, 1, -1, -1, 1, 1, -1, -1, 1, -1]
"coloring", {1, 5, 6, 9, 10}, {2, 3, 4, 7, 8, 11, 12}
"Y2"
"a", [1, -1, -1, -1, 1, -1], "g", [-1, 1, 1, -1, 1, -1, 1, 1, -1, -1, -1, 1]
"coloring", {1, 4, 6, 7, 8, 10, 12}, {2, 3, 5, 9, 11}
"Y2"
"a", [1, -1, -1, 1, -1, -1], "g", [-1, 1, 1, 1, -1, -1, -1, 1, -1, 1, -1, 1]
"coloring", {1, 4, 8, 11, 12}, {2, 3, 5, 6, 7, 9, 10}
"Y2"
"a", [1, -1, 1, -1, -1, -1], "g", [-1, 1, 1, 1, -1, -1, 1, -1, 1, -1, -1, 1]
"coloring", {1, 5, 6, 7, 9, 10, 11}, {2, 3, 4, 8, 12}
"Y2"
"a", [1, 1, -1, -1, -1, -1], "g", [-1, 1, -1, 1, -1, 1, 1, 1, -1, -1, -1, 1]
"coloring", {2, 5, 7, 8, 10, 11, 12}, {1, 3, 4, 6, 9}
"X2"
"a", [1, -1, -1, -1, -1, -1], "g", [-1, 1, 1, 1, -1, -1, 1, 1, -1, -1, -1, 1]
"coloring", {1, 5, 6, 7, 8, 10, 11, 12}, {2, 3, 4, 9}
"Y2"

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FIRST RUN STARTS HERE

```

> NN:=binomial(n,2):J2:=evalm(IdentityMatrix(NN)):uu:=vector(NN,1):UJ:=matrix(n,n,1):unassign('t','e','x','tau'):t:=vector(
> Nmat:=evalm(1/2*UJ-matrix(n,n,(i,j)->1/2*g[i]*g[j]));u2:=vector(NN):c:=1:for i to n-1 do for j from i+1 to n do
u2[c]:=Nmat[i,j]:c:=c+1:od:od:
> q:=evalm(pi&*Nmat)[1]:"RANK",1/(1-q):"PI-R-Nmat",multiply(pi,R,Nmat),"PI-B-Nmat",multiply(pi,B,Nmat);
> AA:=sympow(A,2):D2:=sympow(Detta,2):A2:=evalm(AA+D2):multiply(AA,u2);"det",det(J2-A2):evalm(multiply(A2-J2,u

```



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> NN:=binomial(n,2):J2:=evalm(IdentityMatrix(NN)):uu:=vector(NN,1):UJ:=matrix(n,n,1):unassign('t','e','x','tau'):t:=vector(
> unassign('e','a','w'):pi:=evalm(1/w[1]*linsolve(J-transpose(A),vector(n,0),'r',w)):d:=rank(Delta):`rank of Delta`=d,`for n eq
A`=rank(A):NA:=NullSpace(Matrix(A)):NTA:=NullSpace(Matrix(transpose(A))):nu:=nullity(Delta):zeta:=vector(n,0):u=v
> #apart:=ecliffe(evalm(2*(symult(A,J)+symult(Delta,J)))):liecliff(n):#ydet:=collect(trace(multiply(Y,apart)),[seq(x[k],k=1..n)
> ISX:=NullSpace(Matrix(transpose(evalm(Delta)))):ND:=NullSpace(Matrix(Delta)):
> CA:=r->if r>0 then concat(seq(NA[q],q=1..r)) else "" fi:CTA:=r->if r>0 then concat(seq(NTA[q],q=1..r)) else "" fi:
> "ker A",CA(nullity(A)),`ker Tr A`,CTA(nullity(A)),`ker Delta`,concat(seq(ND[q],q=1..nullity(Delta))),`ker tr
Delta`,concat(seq(ISX[q],q=1..nullity(Delta)))

```

PROCEDURES Sigma diag signs and MATADJ(mat,rownum) are here

```

> sig:=multiply(pi,u):spi:=evalm(pi/sig):Omega:=stackmatrix(seq(spi,q=1..n)):#Hpi:=multiply(spi,F):Fpi:=multiply(spi,QD)

```

J2 and AA are defined here also all ones JJ then PI and EI. NN is n-choose-2.

```

> unassign('x'):#q:=vector(NL):qq:=multiply(q,EI):vv:=linsolve(transpose(EI),spi,'r','x');

```

```

π := [1, 1, 2, 1, 1, 1, 2, 2, 1, 1, 2, 2, 2]

```

```

rank of Delta = 6, for n equals = 12

```

```

rank of A = 6

```

```

"Delta",
⎡ 0  0  -1  0  0  1  0  0  0  0  0  0  0 ⎤
⎢ 0  0  1  0  0  -1  0  0  0  0  0  0  0 ⎥
⎢ 0  0  1  0  0  -1  0  0  0  0  0  0  0 ⎥
⎢ 0  0  0  0  0  0  1  0  0  -1  0  0  0 ⎥
⎢ 0  0  0  0  0  0  -1  0  0  1  0  0  0 ⎥
⎢ 0  0  0  0  0  0  -1  0  0  1  0  0  0 ⎥
⎢ 0  0  0  0  0  0  0  0  0  0  1  -1  -1 ⎥
⎢ 0  0  0  0  0  0  0  0  0  0  1  -1  -1 ⎥
⎢ 0  0  0  0  0  0  0  0  0  0  0  -1  1  ⎥
⎢ 1  -1  0  0  0  0  0  0  0  0  0  0  0  ⎥
⎢ 0  0  0  1  -1  0  0  0  0  0  0  0  0  ⎥
⎢ 0  0  0  0  0  0  0  -1  1  0  0  0  0  ⎥

```

```

"ker A",
⎡ 0  0  -1  0  0  0 ⎤
⎢ 0  0  1  0  0  0 ⎥
⎢ 0  0  0  0  -1  0 ⎥
⎢ 0  0  0  -1  0  0 ⎥
⎢ 0  0  0  1  0  0 ⎥
⎢ 0  0  0  0  1  0 ⎥
⎢ -1  0  0  0  0  0 ⎥
⎢ 0  0  0  0  0  -1 ⎥
⎢ 0  0  0  0  0  1  ⎥
⎢ 1  0  0  0  0  0 ⎥
⎢ 0  -1  0  0  0  0 ⎥
⎢ 0  1  0  0  0  0 ⎥

```

```

, "ker Tr A",
⎡ 0  0  0  0  -1  -1 ⎤
⎢ 0  0  0  0  1  0  ⎥
⎢ 0  0  0  0  0  1  ⎥
⎢ -1  -1  0  0  0  0 ⎥
⎢ 1  0  0  0  0  0  ⎥
⎢ 0  1  0  0  0  0  ⎥
⎢ 0  0  -1  -1  0  0 ⎥
⎢ 0  0  1  0  0  0  ⎥
⎢ 0  0  0  1  0  0  ⎥
⎢ 0  0  0  0  0  0  ⎥
⎢ 0  0  0  0  0  0  ⎥
⎢ 0  0  0  0  0  0  ⎥

```

```

, "ker Delta",
⎡ 0  0  0  0  0  1 ⎤
⎢ 0  0  0  0  0  1 ⎥
⎢ 0  0  1  0  0  0 ⎥
⎢ 1  0  0  0  0  0 ⎥
⎢ 1  0  0  0  0  0 ⎥
⎢ 0  0  1  0  0  0 ⎥
⎢ 0  0  0  1  0  0 ⎥
⎢ 0  1  0  0  0  0 ⎥
⎢ 0  1  0  0  0  0 ⎥
⎢ 0  0  0  1  0  0 ⎥
⎢ 0  0  0  0  1  0 ⎥
⎢ 0  0  0  0  1  0 ⎥

```

```

, "ker tr Delta",

```


$$\begin{bmatrix} 0 & 0 & -1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & -1 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ -1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$spi := \left[\frac{1}{18}, \frac{1}{18}, \frac{1}{9}, \frac{1}{18}, \frac{1}{18}, \frac{1}{9}, \frac{1}{9}, \frac{1}{18}, \frac{1}{18}, \frac{1}{9}, \frac{1}{9}, \frac{1}{9} \right]$$

TEMPLATE HERE

```
> matrans(RR),matrans(BB);count:=0;R:=evalm(RR);B:=evalm(BB):if(rank(A)<>rank(Delta)) then print("NOT A CC
GRAPH");print();else print("CC GRAPH") fi;

> J:=evalm(IdentityMatrix(n));unassign('t','s'):chply:={}:colrs:={}:NSA:=nullspace(A):"NullSpace for
A",NSA;XAX:=symult(A,J):cc:={}:rg:={}:

> AA:=sympow(A,2):EA:=eigenvalues(A):EAV:=map(evalf,[EA]):EVA:=map(abs,EAV):MA:=max(seq(EVA[k],k=1..nops(E
A),EAV));print("abs vals",EVA);print("max",MA);print("charpoly",factor(charpoly(A,t)),"minpoly",factor(minpoly(A,s)));

> N2:=binomial(n,2):J2:=evalm(IdentityMatrix(N2)):u:=vector(n,1):uu:=vector(N2,1):ee:=vector(n,1):for k from 0 to n do
for i in choose(n,k) do ee:=vector(n,1): if (1 in i) then next fi;for j to n do if(j in i) then ee[j]:=-1 fi
od;phi:=diag(seq(ee[q],q=1..n));dl:=multiply(phi,Delta);D2:=sympow(dl,2);A2:=evalm(AA+D2):

> count:=count+1;if( (count mod 20)=0) then

> print('=====');print();

> print(count,ee);fi;sw:=false;if(det(J2-A2)=0) then

> print('=====');print();

> dim:=nops(nullspace(J2-A2));

> if(dim>1) then AB:=abel(A2):u2:=evalm(AB&*uu) ;pi2:=evalm(uu&*AB):print("FIXED POINTS DIM ",dim) else
u2:=evalm(1/x[1]*linsolve(J2-A2,vector(N2,0),'rr',x));pi2:=evalm(1/x[1]*linsolve(J2-transpose(A2),vector(N2,0),'rr',x));
fi;

> vx:=readVec(u2);ux:=evalm(u2/u2[vx[1]]);

> for i to N2 do if ( (ux[i]>1) and (ux[i]<0)) then print("SANDWICH");sw:=true; break;fi od;if(not sw) then
print("RIGHT GROUP") fi;

> m:=max(seq(u2[k],k=1..NN)):NX:=matvec(u2);rh:=multiply(spi,NX):rk:=m/(m-rh[1]):pp:=multiply(NX,u/m):COLR:=read
then colrs:=colrs union {[COLR,rk]}; else if(rk<n) then rg:=rg union {[COLR,rk]} else rg:=rg union {[COLR,rk,"group"]} f
fi;RX:=evalm(A+dl):BX:=evalm(A-dl):

> print("Coloring",COLR,"RANK",rk);print("R",matrans(RX),"B",matrans(BX)); print("pi2",pi2);print("u2",u2,"dim",dim);p
Rk:=sympow(RX,rk):Bk:=sympow(BX,rk):Ak:=evalm(1/2*(Rk+Bk));nk:=binomial(n,rk):jk:=evalm(IdentityMatrix(nk)):u1
print("pi"||rk,pi||rk);print("u"||rk,u||rk);fi; if(iszero(symult(dl,J)-XAX)) then print("COLORING IS CC");cc:=cc union

> print('=====');print();
```


140, [1, 1, -1, 1, 1, 1, 1, -1, 1, -1, 1, 1]

160, [1, 1, 1, -1, 1, -1, 1, 1, 1, 1, -1, 1]

180, [1, 1, 1, 1, -1, -1, 1, 1, 1, -1, 1, 1]

200, [1, 1, 1, 1, 1, -1, -1, 1, 1, -1, 1, 1]

220, [1, 1, 1, 1, 1, 1, -1, 1, 1, -1, -1, 1]

"RIGHT GROUP"

"Coloring", {2, 3, 4, 9}, "RANK", 2

"R", [3, 6, 6, A, 7, 7, B, B, C, 2, 4, 9], "B", [6, 3, 3, 7, A, A, C, C, B, 1, 5, 8]

"pi2", $\left[0, \frac{75}{52}, 0, 0, 0, \frac{5}{13}, \frac{20}{13}, 0, 0, 0, 2, 0, 0, 0, \frac{75}{52}, 0, 0, \frac{20}{13}, \frac{5}{13}, 2, 0, 0, \frac{55}{26}, \frac{75}{52}, 0, 0, 1, \frac{5}{2}, \frac{29}{13}, 0, 0, \frac{55}{26}, 0, 0, \frac{49}{52}, \frac{10}{13}, \frac{20}{13}, 0, \right.$
 $\left. 0, \frac{10}{13}, \frac{49}{52}, 0, 0, 0, \frac{20}{13}, \frac{5}{2}, 1, 0, 0, 0, \frac{29}{13}, 0, \frac{49}{26}, \frac{55}{26}, \frac{40}{13}, 0, 0, \frac{49}{26}, 0, 0, 0, 0, 0, 0, \frac{40}{13}, \frac{49}{26} \right]$

"u2", [1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

240, [1, -1, -1, -1, 1, 1, 1, 1, 1, 1, 1, -1]

260, [1, -1, -1, 1, 1, 1, 1, -1, 1, -1, 1, 1]

280, [1, -1, 1, -1, 1, -1, 1, 1, 1, 1, -1, 1]

"RIGHT GROUP"

"Coloring", {2, 5, 6, 9}, "RANK", 2

"R", [3, 6, 3, 7, A, A, B, B, C, 2, 4, 9], "B", [6, 3, 6, A, 7, 7, C, C, B, 1, 5, 8]

"pi2", $\left[0, 0, 0, 6, \frac{17}{2}, 0, 0, 0, 2, 0, 2, \frac{17}{2}, 6, 0, 0, 2, 0, 0, 0, 2, 0, 0, 1, \frac{17}{2}, 0, 0, 2, 15, 0, 2, 0, 1, 0, 0, \frac{3}{2}, 4, 0, 6, 0, 4, \frac{3}{2}, \right.$
 $\left. 0, 0, 6, 0, 15, 2, 0, 0, 2, 0, 0, 3, 1, 0, 12, 0, 3, 0, 12, 0, 12, 0, 12, 0, 3 \right]$

"u2", [1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 0, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

300, [1, -1, 1, 1, -1, -1, 1, 1, 1, -1, 1, 1]

1, 0, 1, 0, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 0, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

1220, [1, -1, 1, -1, 1, 1, 1, 1, -1, -1, -1, -1]

"RIGHT GROUP"

"Coloring", {2, 5, 6, 7, 9, 11}, "RANK", 2

"R", [3, 6, 3, 7, A, A, C, B, C, 2, 5, 9], "B", [6, 3, 6, A, 7, 7, B, C, B, 1, 4, 8]

"pi2", [0, 0, 0, 0, $\frac{15}{4}$, 0, 4, 0, 1, $\frac{26}{5}$, 0, $\frac{15}{4}$, 0, 0, 0, 1, 0, 4, 0, 0, $\frac{26}{5}$, 0, $\frac{11}{2}$, $\frac{15}{4}$, 0, $\frac{13}{5}$, 0, $\frac{13}{2}$, $\frac{29}{5}$, 0, 0, $\frac{11}{2}$, 0, $\frac{49}{20}$, 0, 2, 4, 0, 0,
2, 0, $\frac{49}{20}$, 0, 0, 4, $\frac{13}{2}$, 0, $\frac{13}{5}$, 0, 0, $\frac{29}{5}$, $\frac{49}{10}$, 0, $\frac{11}{2}$, 8, 0, 0, 0, 0, 0, $\frac{49}{10}$, 0, 0, 0, 8, $\frac{49}{10}$]

"u2", [1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0,
1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

1240, [1, -1, 1, 1, -1, -1, 1, 1, 1, -1, -1, -1]

"RIGHT GROUP"

"Coloring", {2, 5, 7, 9, 10, 11}, "RANK", 2

"R", [3, 6, 3, 7, A, 7, C, B, C, 1, 5, 9], "B", [6, 3, 6, A, 7, A, B, C, B, 2, 4, 8]

"pi2", [0, 0, 0, 0, 1, 2, 0, $\frac{3}{2}$, 0, 0, $\frac{1}{2}$, 1, 0, 0, 0, 0, $\frac{3}{2}$, 0, 2, $\frac{1}{2}$, 0, $\frac{1}{4}$, 0, 1, $\frac{9}{8}$, 0, $\frac{19}{8}$, 0, 0, $\frac{17}{4}$, 0, 0, 0, $\frac{3}{8}$, 0, $\frac{23}{8}$, $\frac{3}{2}$, 0, $\frac{1}{4}$, $\frac{23}{8}$, 0,
 $\frac{3}{8}$, 0, 0, $\frac{3}{2}$, 0, $\frac{19}{8}$, 0, $\frac{9}{8}$, $\frac{17}{4}$, 0, $\frac{3}{4}$, 0, $\frac{1}{4}$, 3, 0, 0, 0, 0, 0, $\frac{3}{4}$, 0, 0, 0, 3, $\frac{3}{4}$]

"u2", [1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 1, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0,
1, 0, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

1260, [1, -1, 1, 1, 1, -1, -1, -1, 1, -1, 1, -1]

1280, [1, 1, -1, -1, -1, -1, -1, 1, 1, 1, -1, 1]

"RIGHT GROUP"

"Coloring", {3, 4, 5, 7, 10, 11}, "RANK", 9

"R", [3, 3, 6, A, A, 7, C, B, B, 1, 5, 9], "B", [6, 6, 3, 7, 7, A, B, C, C, 2, 4, 8]

"pi2", [0, 1, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 2, 2, 1, 1, 2, 2, 2, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1,
1, 2, 1, 1, 2, 2, 2, 1, 1, 2, 2, 2, 0, 1, 1, 1, 1, 1, 1, 2, 2, 2]

"u2", [0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1], "dim", 1

"wpp", [10, 10, 11, 10, 10, 11, 11, 10, 10, 11, 11, 11]

"pi9", [0, 0,

1580, [1, -1, -1, 1, -1, 1, -1, -1, 1, -1, -1, 1]

1600, [1, -1, -1, 1, 1, -1, -1, 1, -1, 1, -1, -1]

1620, [1, -1, 1, -1, -1, -1, -1, 1, 1, -1, -1, 1]

1640, [1, -1, 1, -1, -1, 1, -1, 1, -1, -1, 1, -1]

1660, [1, -1, 1, -1, 1, -1, 1, -1, -1, 1, -1, -1]

"RIGHT GROUP"

"Coloring", {2, 5, 6, 7, 8, 11, 12}, "RANK", 2

"R", [3, 6, 3, 7, A, A, C, C, B, 2, 5, 8], "B", [6, 3, 6, A, 7, 7, B, B, C, 1, 4, 9]

"pi2", $\left[0, 0, 0, 0, \frac{75}{49}, 0, 0, \frac{80}{49}, \frac{20}{49}, \frac{104}{49}, 0, \frac{75}{49}, 0, 0, 0, \frac{20}{49}, \frac{80}{49}, 0, 0, 0, \frac{104}{49}, 0, \frac{110}{49}, \frac{75}{49}, 0, 0, \frac{52}{49}, \frac{130}{49}, \frac{116}{49}, 0, 0, \frac{110}{49}, 0, 0, 1, \frac{40}{49}, \frac{80}{49}, 0, 0, \frac{40}{49}, 1, 0, 0, 0, \frac{80}{49}, \frac{130}{49}, \frac{52}{49}, 0, 0, 0, \frac{116}{49}, 0, 2, \frac{110}{49}, \frac{160}{49}, 0, 0, 2, 0, 0, 0, 0, 0, 0, \frac{160}{49}, 2 \right]$

"u2", [1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

1680, [1, -1, 1, 1, -1, -1, 1, -1, -1, -1, 1, -1]

"RIGHT GROUP"

"Coloring", {2, 5, 7, 8, 10, 11, 12}, "RANK", 2

"R", [3, 6, 3, 7, A, 7, C, C, B, 1, 5, 8], "B", [6, 3, 6, A, 7, A, B, B, C, 2, 4, 9]

"pi2", $\left[0, 0, 0, 0, 1, 2, \frac{3}{2}, 0, 0, 0, \frac{1}{2}, 1, 0, 0, 0, 0, 0, \frac{3}{2}, 2, \frac{1}{2}, 0, \frac{1}{4}, 0, 1, \frac{9}{8}, \frac{19}{8}, 0, 0, 0, \frac{17}{4}, 0, 0, 0, 0, \frac{3}{8}, \frac{23}{8}, \frac{3}{2}, 0, \frac{1}{4}, \frac{23}{8}, \frac{3}{8}, 0, 0, 0, \frac{3}{2}, 0, 0, \frac{19}{8}, \frac{9}{8}, \frac{17}{4}, 0, 0, \frac{3}{4}, \frac{1}{4}, 3, 0, 0, \frac{3}{4}, 0, 0, 0, 0, 0, 0, 3, \frac{3}{4} \right]$

"u2", [1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 1, 1], "dim", 1

"wpp", [6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6, 6]

1700, [1, 1, -1, -1, -1, -1, -1, -1, 1, 1, 1, -1]

1720, [1, 1, -1, -1, -1, 1, -1, -1, 1, -1, -1, 1]

"RIGHT GROUP"

"Coloring", {3, 4, 5, 7, 10, 11, 12}, "RANK", 9


```

[3, 4, 5, 8, 9, 11}, 9], [{2, 4, 7, 9, 10}, 2], [{2, 5, 6, 7, 9, 11}, 2], [{3, 4, 5, 7, 11}, 9], [{3, 4, 5, 7, 10, 12}, 9],
[3, 4, 5, 8, 9, 10, 11}, 9], [{2, 4, 6, 8, 11, 12}, 2], [{3, 4, 5, 7, 10}, 9], [{3, 6, 7, 11}, 9], [{2, 4, 7, 8, 10, 12}, 2],
[3, 4, 5, 7, 12}, 9], [{3, 4, 5, 8, 9, 10}, 9], [{3, 6, 8, 9, 12}, 9], [{2, 4, 8, 10, 11, 12}, 2], [{2, 3, 4, 9}, 2],
[2, 3, 4, 6, 9, 10}, 2], [{2, 3, 5, 7, 8, 12}, 2], [{3, 4, 5, 7, 10, 11, 12}, 9], [{2, 3, 5, 6, 8, 10, 11, 12}, 2],
[2, 3, 5, 7, 9}, 2], [{2, 3, 5, 8, 11, 12}, 2], [{3, 4, 5, 8, 9, 10, 11, 12}, 9], [{3, 4, 5, 7}, 9], [{2, 4, 6, 7, 9}, 2],
[2, 3, 4, 6, 7, 8, 10, 11, 12}, 2], [{3, 6, 8, 9, 10, 11, 12}, 9], [{2, 4, 6, 7, 8, 12}, 2], [{3, 6, 8, 9, 11}, 9]}

```

"SUMMARY: NON-SYNCD CC", 0

{}

```

> nine:={};two:={};for i to 64 do if rg[i][2]=9 then nine:=nine union {rg[i]} else two:=two union {rg[i]} fi; od:
print(nine);print(two);

```

two := {}

```

{[3, 6, 7}, 9], [3, 4, 5, 8, 9}, 9], [3, 6, 8, 9, 11, 12}, 9], [3, 4, 5, 8, 9, 12}, 9], [3, 6, 7, 12}, 9],
[3, 4, 5, 8, 9, 10, 12}, 9], [3, 6, 7, 11, 12}, 9], [3, 4, 5, 8, 9, 11, 12}, 9], [3, 6, 7, 10, 11, 12}, 9],
[3, 4, 5, 7, 11, 12}, 9], [3, 6, 7, 10}, 9], [3, 6, 7, 10, 12}, 9], [3, 6, 8, 9}, 9], [3, 6, 8, 9, 10}, 9], [3, 6, 7, 10, 11}, 9],
[3, 6, 8, 9, 10, 12}, 9], [3, 4, 5, 7, 10, 11}, 9], [3, 6, 8, 9, 10, 11}, 9], [3, 4, 5, 8, 9, 11}, 9], [3, 4, 5, 7, 11}, 9],
[3, 4, 5, 7, 10, 12}, 9], [3, 4, 5, 8, 9, 10, 11}, 9], [3, 4, 5, 7, 10}, 9], [3, 6, 7, 11}, 9], [3, 4, 5, 7, 12}, 9],
[3, 4, 5, 8, 9, 10}, 9], [3, 6, 8, 9, 12}, 9], [3, 4, 5, 7, 10, 11, 12}, 9], [3, 4, 5, 8, 9, 10, 11, 12}, 9], [3, 4, 5, 7}, 9],
[3, 6, 8, 9, 10, 11, 12}, 9], [3, 6, 8, 9, 11}, 9]}

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> nops(two);

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